

Math 29
Factoring

Factor the expression completely.

1. $9x^4 - 4y^2$
2. $x^3 - 1$
3. $3x^2 - 10xy + 8y^2$
4. $10x^2 - 250$
5. $x^3 - 4x^2 - 9x + 36$
6. $4x^3 + 32$
7. $x^{23}y - x^{21}y$
8. $3x^2 - 18x - 21$
9. $4x - 8x^2 - 5x^3$
10. $x^4 - 4x^2 - 45$
11. $(a + 2b)^2 - 25c^{20}$
12. $a^3b - b^7$
13. $8x^6 + 14x^5 - 4x^4$
14. $45x^3y^5 - 5xy^9$
15. $3x^8 - 11x^4 + 6$
16. $3x^8 - 11x^7 + 6x^6$
17. $9x^{34} - (y + 10)^2$
18. $4a^2 - 8ab + 14b - 7a$
19. $10x^5 + 40x^3 - 50x$
20. $x^6 + 3x^5 - 10x^4$
21. $x^6 - 4x^3 - 5$
22. $1000a^3 + 27b^6$
23. $x^{12} + 4x^6 - 32$
24. $(3x - 11)^3 + 27$
25. $(x^2 - 25)^7$
26. $x^{\frac{5}{2}} - 9x^{\frac{1}{2}}$
27. $8x^{\frac{8}{3}} - x^{-\frac{1}{3}}$
28. $2x^{\frac{4}{3}} - 7x^{\frac{1}{3}} - 4x^{-\frac{2}{3}}$
29. $2x^{\frac{2}{3}} - 3x^{\frac{1}{3}} - 20$
30. $x^{-\frac{3}{2}} + 2x^{-\frac{1}{2}} + x^{\frac{1}{2}}$
31. $11x^5(2x + 3)^7 - 4x(2x + 3)^8$
32. $(2x - 7)^5(x - 8)^{30} + (2x - 7)^4(x - 8)^{31}$
33. $10x^{15}(x - 6)^{-4} - 8x^{14}(x - 6)^{-3}$
34. $3x^{-\frac{1}{2}}(4x + 3)^{\frac{5}{4}} + x^{\frac{3}{2}}(4x + 3)^{\frac{1}{4}}$
35. $5(x + 8)^7(9x + 2)^{10} - 10(x + 8)^8(9x + 2)^{11}$
36. $5\sin^2 \theta - 3\sin \theta$
37. $\csc^2 x - 3\csc x - 28$
38. $3\tan^2 2x - 2\tan 2x - 1$
39. $4\sin^2 t \cos t - \cos t$
40. $9e^{7x} - 5e^{6x}$
41. $x^2e^{2x} + 5xe^{2x} - 6e^{2x}$
42. $e^{2x} - 6e^x + 8$

Answers

1. $(3x^2 - 2y)(3x^2 + 2y)$ 2. $(x-1)(x^2 + x + 1)$ 3. $(3x - 4y)(x - 2y)$
4. $10(x+5)(x-5)$ 5. $(x-4)(x+3)(x-3)$ 6. $4(x+2)(x^2 - 2x + 4)$
7. $x^{21}y(x+1)(x-1)$ 8. $3(x-7)(x+1)$
9. $-x(5x-2)(x+2)$ OR $x(2-5x)(2+x)$ 10. $(x^2 + 5)(x+3)(x-3)$
11. $(a+2b+5c^{10})(a+2b-5c^{10})$ 12. $b(a-b^2)(a^2 + ab^2 + b^4)$
13. $2x^4(4x-1)(x+2)$ 14. $5xy^5(3x+y^2)(3x-y^2)$
15. $(3x^4 - 2)(x^4 - 3)$ 16. $x^6(3x-2)(x-3)$
17. $(3x^{17} + y + 10)(3x^{17} - y - 10)$ 18. $(a-2b)(4a-7)$
19. $10x(x^2 + 5)(x+1)(x-1)$ 20. $x^4(x+5)(x-2)$
21. $(x^3 - 5)(x+1)(x^2 - x + 1)$ 22. $(10a+3b^2)(100a^2 - 30ab^2 + 9b^4)$
23. $(x^2 + 2)(x^4 - 2x^2 + 4)(x^3 + 2)(x^3 - 2)$ 24. $(3x-8)(9x^2 - 75x + 163)$
25. $(x+5)^7(x-5)^7$ 26. $x^{\frac{1}{2}}(x+3)(x-3)$
27. $x^{-\frac{1}{3}}(2x-1)(4x^2 + 2x + 1)$ 28. $x^{\frac{2}{3}}(2x+1)(x-4)$
29. $(2x^{\frac{1}{3}} + 5)(x^{\frac{1}{3}} - 4)$ 30. $x^{-\frac{3}{2}}(x+1)^2$
31. $x(2x+3)^7(11x^4 - 8x - 12)$ 32. $3(2x-7)^4(x-8)^{30}(x-5)$
33. $2x^{14}(x-6)^{-4}(x+24)$ 34. $x^{-\frac{1}{2}}(4x+3)^{\frac{1}{4}}(x^2 + 12x + 9)$
35. $-5(x+8)^7(9x+2)^{10}(18x^2 + 148x + 31)$ 36. $\sin \theta(5 \sin \theta - 3)$
37. $(\csc x + 4)(\csc x - 7)$ 38. $(\tan 2x - 1)(3 \tan 2x + 1)$
39. $\cos t(2 \sin t + 1)(2 \sin t - 1)$ 40. $e^{6x}(9e^x - 5)$
41. $e^{2x}(x+6)(x-1)$ 42. $(e^x - 4)(e^x - 2)$