Provide a clear and organized presentation. Determine the absolute extrema for $f$ over the closed region bounded by the triangular region whose vertices are $(-2,0),(0,-2)$, and $(0,2)$ if $f(x, y)=\frac{1}{2} x^{2}-x y+\frac{2}{3} y^{3}+x-y+1$. This quiz is Harry Potter-free enforced.

