Provide a clear and organized presentation. Evaluate the following integral:

$$
\int \frac{x^{7}-23 x^{5}+62 x^{4}-82 x^{3}+101 x^{2}-68 x+10}{x^{7}-7 x^{6}+19 x^{5}-33 x^{4}+50 x^{3}-50 x^{2}+32 x-24} d x
$$

