Provide a clear and organized presentation. Show all of your work, give exact values only, and completely simplify your answer. Evaluate the following integral:

$$\int \frac{\sin x - 2\cos x}{2\sin x + \cos x}\,dx$$