Provide a clear and organized presentation. Show all of your work and completely simplify your answer. Solve the following differential equation:

$$
\left(2 y^{3}+11 y^{2}+26 y+24\right) \sqrt{3-x^{2}} \frac{d y}{d x}=x^{2}\left(y^{4}+7 y^{3}+18 y^{2}+27 y+27\right)
$$

