

Use a generating function to determine an explicit formula for the following sequences for which a recurrence relation is given:

$$a_n = 4a_{n-1} + 12a_{n-2} \text{ where } a_0 = 2 \text{ and } a_1 = 1$$