

Provide a clear and organized presentation. Show all of your work, provide exact values only, and completely simplify your answers.

1. (8 pts) If  $a_n = -\sqrt{3}a_{n-1} + 6a_{n-2}$  and  $a_0 = -1$  and  $a_1 = 3$ , then determine an explicit formula for  $a_n$

2. (10 pts) If  $a_n = 3a_{n-1} + 10a_{n-2}$  and  $a_0 = 2$  and  $a_1 = -1$ , then use a generating function to determine an explicit formula for  $a_n$

3. (8 pts) If  $f(x) = \ln x$ , then determine an explicit formula for the  $n^{\text{th}}$  order derivative.

4. (8 pts) Recall the Fibonacci sequence:  $1, 1, 2, 3, 5, 8, 13, \dots$ . Prove that:

$$f_1 + f_3 + f_5 + \dots + f_{2n-1} = f_{2n} \quad \forall n \in \mathbb{N}$$

5. (8 pts) Use *Mathematical Induction* to prove that our formula for computing the sum of the first  $n$  terms of an arithmetic series is valid.

6. (8 pts) Use *Mathematical Induction* to prove that our formula for computing the sum of the first  $n$  terms of a geometric series is valid.