

Provide a clear and organized presentation and justify your answers. Consider the linear transformation $T : M_3(\mathbb{R}) \rightarrow P_5$ defined by:

$$T \left(\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \right) = (a_{11} + a_{12} - a_{13}) + (a_{21} - a_{22} + a_{23})x + a_{33}x^2 + (a_{32} - a_{31})x^3 \\ + \pi(a_{21} - a_{22} + a_{23})x^4 + (a_{11} + a_{12} + a_{13})x^5$$

1. Determine $\text{Ker}(T)$
2. Is T 1-1?
3. Determine $\text{Rng}(T)$
4. Is T onto?