

Provide a clear and organized presentation. Prove each of the following or provide a counterexample.

1. Let V be a vector space for which $V = \text{span}\{\bar{v}_1, \bar{v}_2, \dots, \bar{v}_n\}$ and $\bar{v} \in V$. Is $\{\bar{v}_1, \bar{v}_2, \dots, \bar{v}_n, \bar{v}\}$ a linearly independent set?
2. Let V be a vector space and $\bar{v} \in V$. Under what conditions is $\{\bar{v}\}$ a linearly dependent or independent set?
3. Let V be a vector space and consider $\{\bar{v}_1, \bar{0}\}$. Is $\{\bar{v}_1, \bar{0}\}$ a linearly independent or dependent set?