

Provide a clear and organized presentation. Give exact values only and completely simplify all answers.

1. (10 pts) Determine  $f'(x)$  if  $f(x) = \frac{2x}{3-x^2}$  using our definition of the derivative function (i.e., the limit of a difference quotient).

2. (15 pts) Determine the equation of the tangent line that passes through the point  $(-6,3)$  if the line is tangent to the graph of  $y = f(x)$  where  $f(x) = \sqrt{2-x}$

3. (15 pts) Determine  $\frac{dy}{dx}$  if  $\sqrt{xy} - x^2 = y^3 + \ln(xy)$

4. (10 pts) Find all values of  $x$  for which the tangent line to the graph of  $y = f(x)$  is horizontal if  $f(x) = x + 3\sin x$

5. (21 pts) Find  $y'$ :

i)  $y = \tan^{-1} \frac{1}{x\sqrt{x}}$

ii)  $y = x^2 e^{x^3}$

iii)  $y = \pi^x + x^\pi - e^\pi$

6. (15 pts) Find  $y'$  if  $y = \ln^3 \frac{e^x + e^{-x}}{e^x - e^{-x}}$

7. (7 pts) If  $y = \ln x^\pi$ , determine  $y^{(n)}$

8. (7 pts) Evaluate  $\lim_{x \rightarrow 0} \frac{\tan^2 5x}{\sin^2 3x}$