Provide a clear and organized presentation. Show all of your work and provide exact values only. Completely simplify your answer.

$$y^{3}\left(x^{3}+3x^{2}-4\right)\frac{dy}{dx}=\left(y^{2}+\sqrt{y^{2}+3}\right)\left(x^{4}+5x^{3}+10x^{2}+x-6\right)$$