

- I. Mechanical Systems with Free Oscillation with spring constant and frictional coefficient:
1.  $k = 4 \text{ g/s}^2$ ,  $m = 1 \text{ g}$  where the object is initially pulled down 2 cm and with a downward initial velocity of 2 m/s
  2.  $k = 5 \text{ g/s}^2$ ,  $m = 1 \text{ g}$ ,  $c = 4 \text{ g/s}$  where the object is initially pulled down 2 cm and with a downward initial velocity of 2 m/s
- II. Mechanical Systems with Forced Oscillations:
1.  $k = 25 \text{ g/s}^2$ ,  $m = 1 \text{ g}$ ,  $c = 0 \text{ g/s}$  where the object is initially pulled down 0 cm and with a downward initial velocity of 10 m/s. Consider an external force of  $10\sin 4t$
  2. Consider a system in which our mathematical model is:
    - i)  $y(t) = t \sin t + C_1 \cos \omega t + C_2 \sin \omega t$
    - ii)  $y(t) = e^{-at} (C_1 \cos bt + C_2 \sin bt) + A \cos(\omega t - \phi)$
- III. RLC Circuits:
1.  $R = 20 \Omega$ ,  $L = 1 \text{ henry}$ ,  $C = 0.005 \text{ farads}$ . The voltage is shorted out at  $t = 0$  and there is initially a charge of 10 coulombs on the capacitor and no current. How many seconds will it take for the amplitude to be reduced by 99%?
  2.  $R = 1 \Omega$ ,  $L = \frac{1}{2} \text{ henry}$ ,  $C = \frac{2}{3} \text{ farads}$ . The voltage is given by  $E(t) = \cos t$ .
- IV. Examples of Higher Order Differential Equations with Non-Constant Coefficients:
1.  $x^2 \frac{d^2 y}{dx^2} + \frac{7}{2} x \frac{dy}{dx} - \frac{3}{2} y = 0$  with  $x > 0$
  2.  $x^2 \frac{d^2 y}{dx^2} + \frac{5}{3} x \frac{dy}{dx} + \frac{5}{9} y = 0$  with  $x > 0$
  3.  $x^2 \frac{d^2 y}{dx^2} + 2x \frac{dy}{dx} = x^{-1}$  with  $x > 0$

4.  $x^2 \frac{d^2 y}{dx^2} - x \frac{dy}{dx} + y = x^3 \ln x$  with  $x > 0$