Provide a clear and organized presentation. Show all of your work and completely simplify your answer. Evaluate the following integrals:

1. $\int \frac{e^{2 x}}{e^{2 x}+e^{-x}} d x$
2. $\int \frac{1}{x^{2}} \sin \frac{1}{x} \cos ^{2} \frac{1}{x} d x$
