Provide both a clear and organized presentation and show all of your work. Evaluate the following integral:

$$
\int \frac{\cos (\ln x)}{x \sqrt{\sin ^{2}(\ln x)-1} \ln ^{4}\left(\sin (\ln x)+\sqrt{\sin ^{2}(\ln x)-1}\right)} d x
$$

