Provide a clear and organized presentation. Determine the equation(s) of the tangent lines to the graph of $y = f(x)$ that pass through the point $(3, -10)$ if $f(x) = \dfrac{2x}{x-3}$. Put your answer(s) in *slope-intercept* form.