Decide whether each of the following is true without using a calculator or long division (all numbers on this quiz are natural numbers, unless otherwise stated):

1. If a natural number is divisible by 4 and by 14 , it is divisible by 56 .
2. $40 \mid 5$ !
3. 576 is prime.
4. $a^{m} b^{n} \mid a^{p} b^{m}$ if $m<n<p$.
5. $\quad a^{m} b^{n} \mid a^{n} b^{p}$ if $m<n<p$.
6. If $3 \mid b$ and $4 \mid b$, then $12 \mid b$.
7. If $12 \mid a b$, then $12 \mid a$ or $12 \mid b$.
8. The prime factorization of $234,547,84$ includes 2 three times.
9. $\quad 9$ is a factor of 243,912 is divisible by 9 .
10. If $5 \mid \mathrm{b}$ and $7 \mid \mathrm{b}$, then $35 \mid \mathrm{b}$.
