

Consider the following sets. Determine whether the properties of a ring I have indicated are satisfied.

1. $R = \{r\sqrt{2} \mid r \in \mathbb{Q}\}$. Check closure for both operations and one of the distributive properties/laws.
2. $R = \left\{ \frac{1}{n} \mid n \in \mathbb{N} \right\}$. Check closure for both operations, and of the distributive properties, and the existence of an additive identity (property *c* on page 673)